The Effect of Various Soil Hydraulic Property Estimates on Soil Moisture Simulations

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Models of water movement in unsaturated soils require accurate representations of the soil moisture retention and hydraulic conductivity curves; however, commonly used laboratory methods and pedotransfer functions (PTFs) are rarely verified against field conditions. In this study, we investigated the effects of using soil hydraulic property information obtained from different measurement and estimation techniques on one-dimensional model predictions of soil moisture content. Pairs of time domain reflectometry waveguides and tensiometers were installed at two depths in the side of a soil pit face to obtain in situ measurements. Undisturbed soil samples were taken near the instruments and subjected to particle size analysis, multistep outflow (MSO), and falling-head permeability tests to obtain estimates of the soil moisture retention curves. Three scaling methods were then applied to improve the fit of the various estimates to the field data. We found that soil hydraulic property estimates obtained from inverse methods lead to the best simulations of soil moisture dynamics, and that laboratory MSO tests or commonly used PTFs perform poorly. These laboratory and PTF estimates can be dramatically improved, however, by simply constraining the range of possible moisture contents to the minimum and maximum measured in the field. It appears that this method of scaling PTF results can be used to obtain soil hydraulic property inputs of sufficient accuracy for plot-scale modeling efforts without requiring expensive laboratory or in situ tests.

ABBREVIATIONS: DOY, day of the year; MR, mean residual; MSO, multistep outflow; PTF, pedotransfer function; RB, Rawls and Brakensiek (1985); TDR, time domain reflectometry; WOE, Wösten et al. (1999).
Materials and Methods

Field Measurements

This study was conducted in the Treeline catchment in the Dry Creek Experimental Watershed near Boise, ID (Fig. 1). The Treeline catchment has a mean elevation of 1620 m, a relief of 35 m, and a northwest–southeast orientation with soil formed in place from weathering of the granitic bedrock. A meteorological station on the northeast-facing slope records precipitation, snow depth, air temperature, relative humidity, wind speed, wind direction, incoming solar radiation, net longwave radiation, soil temperature, and soil moisture on a CR10X datalogger (Campbell Scientific, Logan, UT). For detailed information about instrumentation of the site, refer to McNamara et al. (2005) and Williams et al. (2008).

Several soil pits were dug to the bedrock interface at 5- to 10-m intervals upslope from the stream in 2002 as part of a study to investigate hydraulic connections between hillslopes and streams. In the present study, we restricted the analysis to one-dimensional infiltration in one pit, SU10, to focus on soil hydraulic properties rather than hillslope hydrology. The naming convention indicates that the pit is on the south-facing slope, located 10 m above the stream.

At SU10, pairs of time-domain reflectometry (TDR) waveguides and tensiometers were installed horizontally at 15 and 52 cm below the ground surface into the side of the soil pit. The soil–bedrock interface was a few centimeters below the lowest sensor. The TDR100 waveguides were 30 cm in length; coaxial multiplexers and CR10X dataloggers (Campbell Scientific, Logan, UT) were used to collected hourly data. Errors in soil moisture measurements are difficult to quantify because, in addition to instrument accuracy, errors may arise from various site-specific conditions; however, TDR is considered to be among the best methods of in situ soil moisture measurement (Blonquist et al., 2005). Complementary measurements of soil water pressure head were made with automated tensiometers constructed from remote soil moisture samplers (Soil Moisture Equipment, Goleta, CA) and 34.47-kPa (5-psi, ±0.2% of full-scale output) differential pressure transducers (Sensym ASCX05DN, Honeywell, Morristown, NJ). Undisturbed soil samples (5.4 cm in diameter and 3 cm in length) were taken from each pit at the same depth as the instruments during installation, 20 to 50 cm away from the sensor pairs so as not to influence subsequent measurements. In 2005 and 2006, additional undisturbed soil cores were taken from new pits dug 100 cm away from the instrumented pit and at the approximate depths of the TDR–tensiometer pairs for MSO and saturated hydraulic conductivity ($K_s$) testing.

Laboratory Measurements

The original SU10 samples, and those taken later, were analyzed for particle size distribution via mechanical sieving and hydrometer analysis (ASTM, 2007). Three to five falling-head permeability tests (Reynolds et al., 2002) were performed on two undisturbed core samples from each soil depth to measure $K_s$. Soil samples were saturated from the bottom in a constant-head basin for a minimum of 2 d before testing. The temperature of the water was held constant at 22.5 ± 1.5°C. Multistep outflow tests were also performed. A manual hanging column test was run on one of the undisturbed cores to determine the soil moisture retention curve, $\theta(h)$ (Dane and Hopmans, 2002). The soil sample was placed in a Tempe cell on a 0.1-MPa porous plate and saturated slowly from the bottom with a 0.005 mol L$^{-1}$ CaSO$_4$ and 0.3 g L$^{-1}$ thymol solution for several days (Klute and Dirksen, 1986). Increasingly negative pressure heads (−10, −20, −30, −40, −50, −60, −70, −80, −90, −110, −130, and −150 cm of water) were applied by lowering a burette below the Tempe cell. The other sample was tested using a pressure cell; positive pressure was applied incrementally at the top of the soil sample in similar magnitude steps. Previous studies have shown the two methods to produce comparable results (Figuera and Gribb, 2009). At each step, cumulative outflow volume was measured with time until outflow ceased (24–48 h). After 48 h at the final applied pressure step, the wet weights of
the samples were obtained. The samples were subsequently oven dried at 105°C for 24 h to obtain the dry soil weights. Soil moisture contents were back-calculated at each step to obtain points on the $\theta(h)$ curve.

**Soil Hydraulic Properties**

The van Genuchten (1980) and Mualem (1976) models for the unsaturated soil hydraulic properties were used in this work:

$$\theta(h) = \frac{\theta_s - \theta_r}{[1 + (\alpha |h|)^{n/\alpha}]^m} + \theta_r, \quad h < 0$$  \[1\]

$$\theta(h) = \theta_s, \quad h = 0$$

$$K(h) = \frac{K_s}{[1 + (\alpha |h|)^{n/\alpha}]^m}, \quad h < 0$$  \[2\]

where $\theta(h)$ is the volumetric moisture content at a specific pressure head ($h$); $\theta_s$ and $\theta_r$ are the residual and saturated volumetric moisture contents, respectively; $\alpha$ (cm$^{-1}$), $n$, and $m$ (where $m$ is typically set equal to $1 - 1/n$) are the van Genuchten fitting parameters; $K(h)$ is the hydraulic conductivity at a specific pressure head; $K_s$ (cm d$^{-1}$) is the saturated hydraulic conductivity; and $l$ is the pore connectivity parameter that is typically set equal to 0.5 (Mualem, 1976) but can be optimized. Hydraulic parameters for each layer at SU10 were obtained using several techniques: (i) in situ measurements, (ii) laboratory MSO and falling-head tests, (iii) the use of PTFs based on neural networks and multiple linear regression, and (iv) inversion of field data. In addition, we explored three methods for scaling the MSO and PTF measurements or estimates with field information to improve their fits to the in situ data.

**Fit of In Situ Data**

Time domain reflectometry soil moisture content and tensiometric head data measured in situ were fitted to Eq. [1] with RETC (van Genuchten et al., 1991), a nonlinear least squares fitting computer code. Hydraulic conductivity curves were estimated using Eq. [2] and the van Genuchten (1980) parameters $\alpha$ and $n$ for the in situ data, paired with $K_s$ values obtained from laboratory falling-head tests. The $l$ parameter was set equal to 0.5. The in situ data served as the basis of comparison for all other techniques described below.

**Scaled In Situ**

Basile et al. (2003) asserted that differences between retention curves measured in the field and in the laboratory are due to differences in imposed boundary conditions. In the case of field application of the instantaneous profile method (Watson, 1966), wetting occurs from the top down, whereas laboratory MSO or evaporation method testing begins with slowly wetting core samples from the bottom. These differences in the mode of water application lead to the generation of different hysteretic branches of the retention curve, with the laboratory drainage curves yielding the highest moisture contents. Basile et al. (2003) proposed combining the estimates of $\theta_s$ and the $\alpha$ parameter (from the results of fitting the moisture content and pressure head readings obtained during the "early" stages of an instantaneous profile method test to Eq. [1]) with the hydraulic parameters obtained via laboratory evaporation experiments (e.g., $\theta_s$ and $n$) to reduce the period during which field measurements are taken. As our laboratory retention curves also showed much higher moisture contents than field measurements for the same pressure heads, we combined the estimates of $\theta_s$ and the $\alpha$ parameter from MSO tests with $\theta_s$ and $n$ obtained from fitting the in situ moisture content and pressure head data collected under natural precipitation conditions.

**Multistep Outflow Tests**

The results of MSO tests were also fit with RETC to obtain parameter values for Eq. [1]. Hydraulic conductivity curves were estimated by using Eq. [2] and the van Genuchten (1980) parameters $\alpha$ and $n$ derived from the MSO test with $K_s$ from falling-head tests. Parameter $l$ was again set equal to 0.5.

**Pedotransfer Functions**

We applied two neural network based PTFs to predict the parameters in Eq. [1] and [2] from soil particle size and bulk density data, and in some cases, organic C content. The first PTF, Rosetta (Schaap et al., 1998, 2001), a public domain code, is based on a wide range of soil types consisting of 2134 soil samples, of which the gravel content is not documented (but probably minimal). This PTF was selected due to its widespread use and availability.

Rosetta requires inputs of percentages of sand (0.05–2 mm), silt (0.002–0.05 mm), and clay (<0.002 mm) and bulk density. Our soil samples had appreciable gravel contents, but since Rosetta does not account for gravel, these percentages were normalized to 100%. The values of $\theta_s$ and $\theta_r$ predicted by Rosetta were then corrected for the gravel dead volume, which was assumed not to participate in the water storage capacity of the soil (Bouwer and Rice, 1983):

$$\theta_b = (1 - V_g)\theta_r$$  \[3\]

where $\theta_b$ is the volumetric moisture content of the gravel–soil mixture (m$^3$ m$^{-3}$), $V_g$ is the volume fraction of the gravel (m$^3$ m$^{-3}$), and $\theta_r$ is the volumetric moisture content of the soil minus the gravel (m$^3$ m$^{-3}$).

The second neural network based PTF used was previously developed for coarse-textured soils, similar to those at the Dry Creek Experimental Watershed. This PTF, called the Hanford PTF here, was created for soils of the Hanford Formation (Hanford, WA) (Ye et al., 2007; Schaal et al., 2003). Gravel percentages of this data set ranged between 0 and 18%, with an average of 1.5% (Schaal, personal communication, 2007).

Two multiple linear regression based PTFs were also applied, based on their successful use in other studies (e.g., Chanzy et al., 2008). The Rawls and Brakensiek (1985) PTF (RB) was created using the Soil Conservation Service database, which contains data from thousands of U.S. agricultural soils and is applicable for soils with sand percentages between 5 and 70%, and clay between 5 and 60%. The Wösten et al. (1999) model (WOE) was based on soils data from several European countries. Although the minimum and maximum percentages of the sand and clay particle sizes were not specifically stated, the soil data used in
the PTF ranged from coarse to very fine materials. The Wösten model accounts for particle size, bulk density, and organic C content. As only the Hanford PTF accounts for gravel content, the percentages of sand, silt, and clay were normalized to neglect the gravel content of the samples, and Eq. [3] was used to correct the moisture contents accordingly for the Rosetta, RB, and WOE PTFs.

Scaling

Given the less-than-optimal fit of the in situ data by the MSO and PTF curves (see below), we attempted to improve these fits and ultimately the predictions of soil moisture contents with time by “scaling” the predicted moisture retention curves described above to the range of moisture contents actually observed in the field. To do this, we tried two approaches in addition to the Basile scaling method discussed above. First, we replaced the predicted values of \( \theta \) and \( \theta_i \) for all of the above \( \theta(b) \) curves with the maximum and minimum moisture contents measured at the sensor locations of interest. These are referred to hereafter as the S1 curves, or field-scaled estimates (e.g., RosettaS1 and so on). Second, we set \( \theta_i \) equal to the field-measured value as before, but calculated the appropriate \( \theta_i \) by solving Eq. [1] for \( \theta_i \) for a known point on the in situ retention curve at the dry end of the range of measured values (for SU10, the lowest reliable measurement for pressure head was approximately \(-300\) cm). We refer to these as the S2 curves (RosettaS2, etc.). Thomasson et al. (2006) applied a similar approach to scale unsaturated hydraulic conductivity curves measured on soil cores in the laboratory by using a single field measurement of unsaturated hydraulic conductivity at a known moisture content to replace \( K_i \) as the matching point.

The accuracy of the various soil moisture retention curves compared with the in situ measurements was assessed by calculating the RMSE:

\[
\text{RMSE}_{\theta(b)} = \sqrt{\frac{1}{K} \sum_{j=1}^{K} \left( \theta(b)_j - \hat{\theta}(b)_j \right)^2}
\]

where \( \theta(b)_j \) and \( \hat{\theta}(b)_j \) are the measured and predicted volumetric moisture contents for \( K = 31 \) points along the moisture retention curve from \( b = 0 \) to \( b = -300 \) cm.

Soil Moisture Modeling

To compare the effects of different soil hydraulic property inputs, we simulated the one-dimensional soil moisture dynamics in SU10 from 27 Feb. to 6 May 2003 (Days of the Year [DOY] 58–126) when the soil was in a wet state, after the primary snowmelt event and before the spring dry-down period (Fig. 2). The primary snowmelt event occurred in January, after which the catchment received intermittent rain and snow for the remainder of the winter.

We used HYDRUS-1D, a public domain, unsaturated–saturated flow and inversion code for one-dimensional problems (Šimůnek et al., 2005; available at www.pc-progress.cz/Fr_Hydrus1D.htm [verified 21 Dec. 2008]). The model solves the Richards (1931) equation for one-dimensional vertical water flow:

\[
\frac{\partial}{\partial z} \left[ K(b) \left( \frac{\partial h}{\partial z} + 1 \right) \right] - S = \frac{\partial \theta}{\partial t}
\]

where \( K(b) \) is the unsaturated hydraulic conductivity (cm s\(^{-1}\)) as a function of \( b \) (cm); \( \theta \) is the volumetric moisture content (m\(^3\) m\(^{-3}\)) as a function of pressure head; \( z \) is the spatial coordinate (cm) positive upward; and \( S \) (m\(^3\) m\(^{-3}\) s\(^{-1}\)) represents the root water extraction rate, defined by Feddes et al. (1978) as

\[
S(b,z) = \alpha(h) S_{\text{max}}(h,z)
\]

where \( \alpha \) is a dimensionless water stress reduction factor as a function of pressure head \( h \) (cm) (unrelated to the \( \alpha \) parameter of Eq. [1]). \( S_{\text{max}} \) (m\(^3\) m\(^{-3}\) s\(^{-1}\)) is the maximum possible root water extraction rate when soil water is not limiting, and \( z \) is the soil depth (cm). No detailed measurements of the vegetation parameters, except maximum rooting depth (Williams, 2005), were conducted on the vegetation at the Treeline site, so the S-shaped water stress response function (van Genuchten, 1987) was used:

\[
\alpha(h) = \frac{1}{1 + \left( h/h_{50} \right)^n}
\]

where \( h_{50} \) is the pressure head at which root water uptake is reduced by 50% and \( p_1 \) is an adjustable parameter. In our study, the values of \( p_1 = 3 \) and \( h_{50} = -3000 \) cm were used. The \( h_{50} \) value...
was set equal to a value used for grass in another arid region study (Guan, 2005).

The air phase was assumed to play an insignificant role in the liquid flow process, and water flow due to thermal gradients was neglected. Following the work of Vogel et al. (2000), we used Eq. [2] with a small non-zero air-entry value of −2 cm. The use of a small air-entry pressure head has little effect on the character of the soil moisture retention curve, but provides better numerical stability for small values of $n$.

The soil profile at SU10 was discretized in 0.5-cm increments from the soil surface to the location of the lower tensiometer (52 cm below the ground surface). The soil profile was modeled as a two-layer system with differing soil hydraulic properties (0–24 and 24–52 cm). This modeling domain was then used for subsequent direct and inverse simulations with the different soil hydraulic property estimates described above.

An atmospheric boundary condition was imposed on the soil surface to account for precipitation and evapotranspiration. This boundary condition in HYDRUS-1D does not account for surface runoff, which was not observed at the site during the periods of interest. Since HYDRUS-1D does not include a snowmelt component, we used the Simultaneous Heat and Water (SHAW) model (Flrichinger et al., 1996) to capture the appropriate timing of soil water input from mixed-phase precipitation and create the input file for HYDRUS-1D. The SHAW model determines if the precipitation is rain or snow depending on air temperature and simulates the melt of accumulated snow using an energy balance approach. Except for the snowmelt event in early March 2003, precipitation was predominantly rain with occasional minor snow events (Fig. 2). The bottom boundary was set equal to the measured pressure heads at the lower tensiometer and the initial conditions for each layer were assigned to the moisture contents measured by the TDR probes.

Effective hydraulic parameters for SU10 were obtained by inversion by minimizing an objective function, $\Phi$, that expressed the differences between modeled and measured moisture at the sensor locations (15 and 52 cm) and the pressure head at the upper sensor location during two short spring precipitation events in 2003, 24–31 March and 2–6 May (DOY 83–90 and 122–126, respectively; Fig. 2). These periods were selected because they followed snowmelt and subsequent tensiometer de-airing, and ran from the beginning of precipitation to the time when the soil moisture content returned to initial conditions. In both events, precipitation occurred as a mixture of rain and snow. The objective function was defined as (Šimůnek et al., 2005)

$$\Phi(b,q,p) = \sum_{j=1}^{m} \sum_{i=1}^{n_j} | q_j^*(z,t) - q_j^e(z,t,b) |^2$$

where the right-hand side represents deviations between the measured ($q_j^*$) and calculated ($q_j^e$) moisture contents at the two measurement depths and the pressure head at the upper sensor location; $m$ is the number of different sets of measurements; $n_j$ is the number of measurements in a particular measurement set; $q_j^*(z,t)$ represents a specific measurement at time $t$ for the $j$th measurement set at depth $z$; $q_j^e(z,t,b)$ are the corresponding model predictions for the vector of estimated parameters $b (\theta, \alpha, n, K_c)$; and the weighting factor, $v_j$, is given by the inverse of the number of measurements multiplied by the variance of those observations (Clausetniter and Hopmans, 1995). The parameters $l$ and $\theta_*$ were not optimized to simplify the inversion process.

To achieve stable estimates, parameters were optimized in a sequential fashion as suggested by Šimůnek and van Genuchten (1996). The estimated parameters obtained from the inversion of Event 1 (DOY 83–91) data were used as initial estimates for the inversion of Event 2 (DOY 122–126) data. We then used the estimated parameters from the inversion of Event 2 data as initial estimates, and inverted the Event 1 data once more to obtain the final effective soil hydraulic parameters for the SU10 profile. These parameter sets were then used to predict the soil moisture at the two sensor locations and the pressure head at the shallow sensor location for an extended period (27 Feb.–6 May 2003).

The goodness of fit of the various simulations was quantified using the RMSE values (Eq. [9]) calculated based on the predicted vs. measured moisture contents at both sensor locations for the entire simulation period. Systematic errors between measurements and predictions were evaluated with mean residual (MR) values (Eq. [10]):

$$\text{RMSE}_{\theta(t)} = \sqrt{\frac{1}{L} \sum_{j=1}^{L} [\theta(t) - \hat{\theta}(t)]^2}$$

$$\text{MR}_{\theta(t)} = \frac{1}{L} \sum_{j=1}^{L} [\theta(t) - \hat{\theta}(t)]$$

where $L$ is the number of estimated and measured values, and $\theta(t)$ and $\hat{\theta}(t)$ are the measured and predicted volumetric moisture contents at both depths for hourly time steps during the extended simulation period. Mass balance errors for simulations were also computed.

As one of the measures of accuracy of soil hydraulic parameters estimates, we also evaluated the predicted cumulative soil water flux at the bottom of the profile for the different sets of hydraulic parameter inputs.

## Results

### Physical Properties

The physical properties of the soil samples with depth at SU10 are presented in Table 1. All soil samples were classified as gravelly sands according to the USDA textural classification system (Soil Survey Staff, 1975). Among the tested samples, gravel content ranged from 15 to 27% in the shallow (0–24 cm) and 13 to 38% in the deep (24–52 cm) soil layers and the combined silt and clay fraction ranged in value from 1 to 13%.

<table>
<thead>
<tr>
<th>Soil layer</th>
<th>Core depth</th>
<th>Bulk density</th>
<th>Particle density</th>
<th>Gravel</th>
<th>Coarse sand</th>
<th>Fine sand</th>
<th>Silt</th>
<th>Clay</th>
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<td>0–24</td>
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<td>55.4</td>
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<th>cm</th>
<th>g/cm$^3$</th>
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<td>1.60</td>
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</table>
Retention Curves

Soil moisture retention curves for each layer were estimated from inversion of the field data with Eq. [8], MSO data, the Basile et al. (2003) scaling approach, and the two additional scaling approaches described above: S1, in which the field-measured maximum and minimum $\theta$ values were used to replace $\theta_s$ and $\theta_r$, and S2, in which the field-measured maximum $\theta$ value was used to replace $\theta_s$ and $\theta_r$ was calculated by fixing a point at the dry end of the in situ retention curve (Fig. 3 and 4). The soil hydraulic parameters are listed in Table 2, and the RMSE values (Eq. [4]) describing the fits of the inversely estimated, laboratory-measured, or PTF-predicted curves to the in situ retention data are shown in Table 3. The $\theta(h)$ curves obtained from the various methods show

Fig. 3. Moisture content as a function of pressure head for the shallow soil layer (0–24 cm) at Pit SU10 as determined by several estimation and measurement techniques: (a) curves from Rosetta, Rawls and Brakensiek (RB), Wösten (WOE), and Hanford pedotransfer functions, multistep outflow (MSO), Basile scaling, and inversion of field data obtained with initial estimates from these sources vs. in situ data; (b) saturated ($\theta_s$) and residual ($\theta_r$) volumetric moisture contents replaced by field-measured values (S1 scaling approach); and (c) $\theta_s$ replaced by field-measured values and $\theta_r$ calculated by fitting a point on the retention curve near −300 cm (S2 scaling approach).

Fig. 4. Moisture content as a function of pressure head for the deep soil layer (24–52 cm) at Pit SU10 as determined by several estimation and measurement techniques: (a) curves from Rosetta, Rawls and Brakensiek (RB), Wösten (WOE), and Hanford pedotransfer functions, multistep outflow (MSO), Basile scaling, and inversion of field data obtained with initial estimates from these sources vs. in situ data; (b) saturated ($\theta_s$) and residual ($\theta_r$) volumetric moisture contents replaced by field-measured values (S1 scaling approach); and (c) $\theta_s$ replaced by field-measured values and $\theta_r$ calculated by fitting a point on the retention curve near −300 cm (S2 scaling approach).
significant variability, as observed in other studies (Mallants et al., 1997; Gribb et al., 2004; Green et al., 2005; Chanzy et al., 2008). As expected, the $\theta(h)$ curves obtained from inversion yielded the best RMSE$_{\theta(h)}$ values (0.003–0.020 m$^3$ m$^{-3}$) for fit to the in situ retention data (Table 3, Fig. 3a and 4a) for both layers. It is important to note, however, that we were able to successfully invert the field data because we had information about bottom boundary conditions as well as measured moisture content and pressure heads in both layers. A lack of knowledge of the bottom boundary conditions would yield inversely estimated parameters that would depend on the assumed boundary conditions.

For the shallow layer, the MSO $\theta(h)$ curve has a similar appearance to the in situ data, but $\theta$ values are consistently higher than those measured in the field (Fig. 3a), with RMSE$_{\theta(h)} = 0.068$ m$^3$ m$^{-3}$, consistent with the observations of Green et al. (2005) and Basile et al. (2003), who also found that laboratory-derived curves overestimated the moisture content for a given pressure head when compared with field measurements. The Basile approach yielded a similar curve (RMSE$_{\theta(h)} = 0.049$ m$^3$ m$^{-3}$). The $\theta(h)$ curves predicted by the Hanford, WOE, and RB PTFs are similar to each other, consistently overestimating the moisture content of the soil, but to a lesser degree as the pressure head decreased toward ~300 cm (RMSE$_{\theta(h)} = 0.044$–0.052 m$^3$ m$^{-3}$). Rosetta also initially overestimated the moisture content from saturation to approximately ~70 cm, and then underestimated $\theta(h)$ values for lower pressure heads [RMSE$_{\theta(h)} = 0.05$ m$^3$ m$^{-3}$].

When the $\theta_s$ and $\theta_r$ values were scaled to the maximum and minimum measured moisture contents as described above (scaling approach S1; Table 3 and Fig. 3b), all of the fits of the curves to the in situ data in the shallow layer were much improved; the Rosetta$_S1$, and MSO$_S1$ curves are the best, with RMSE$_{\theta(h)}$ values of 0.006 and 0.01 m$^3$ m$^{-3}$ (Table 3). The fit of the Hanford, RB, and WOE curves were further improved using the second scaling approach (S2; Fig. 3c) with RMSE$_{\theta(h)}$ values ranging from 0.003 to 0.011 m$^3$ m$^{-3}$ (Table 3).

In the deep layer (24–52 cm below the ground surface), as with the shallow layer, the MSO curve has a similar curvature as the in situ curve, but with elevated moisture contents for given pressure head values [RMSE$_{\theta(h)} = 0.039$ m$^3$ m$^{-3}$]. The Basile curve lies between the MSO and in situ curves [RMSE$_{\theta(h)} = 0.016$ m$^3$ m$^{-3}$]. The $\theta(h)$ curves predicted by the Rosetta, WOE, and RB PTFs yielded even poorer representations of the in situ $\theta(h)$ curve than they did for the shallow layer [RMSE$_{\theta(h)} = 0.059$–0.117 m$^3$ m$^{-3}$] (Table 3, Fig. 4a). These PTFs significantly overestimated the maximum moisture contents and then greatly underestimated the lowest measured moisture contents; the curves do not follow the in situ data at all. On the other hand, the Hanford PTF fits much better. It initially underestimated the saturated moisture content, but it yielded a curve that is similar to the in situ data and that improved as the pressure head decreased [RMSE$_{\theta(h)} = 0.02$ m$^3$ m$^{-3}$] (Fig. 4a).

In summary, only the Hanford PTF and Basile curves provided reasonable approximations of the in situ behavior (Fig. 4a). Replacing $\theta_s$ and $\theta_r$ with field-measured values (S1 scaling) again improved the fits of all curves except the Hanford$_S1$ curve, but not to the extent seen for the shallower depth (RMSE values ranged from 0.014–0.028 m$^3$ m$^{-3}$ for WOE$_S1$, RB$_S1$, MSO$_S1$, and Rosetta$_S1$, Table 3, Fig. 4b). When the hydraulic parameters were

<table>
<thead>
<tr>
<th>Source of hydraulic parameters</th>
<th>Depth</th>
<th>$\theta_r$</th>
<th>$\theta_s$</th>
<th>$\alpha$</th>
<th>$n$</th>
<th>$l$</th>
<th>$K_s$</th>
</tr>
</thead>
<tbody>
<tr>
<td>In situ data</td>
<td>0–24</td>
<td>0.07</td>
<td>0.20</td>
<td>0.040</td>
<td>1.70</td>
<td>0.50</td>
<td>692‡</td>
</tr>
<tr>
<td></td>
<td>24–52</td>
<td>0.06</td>
<td>0.27</td>
<td>0.026</td>
<td>1.40</td>
<td>0.50</td>
<td>320†</td>
</tr>
<tr>
<td>Multistep outflow</td>
<td>0–24</td>
<td>0.14</td>
<td>0.35</td>
<td>0.121</td>
<td>1.62</td>
<td>0.50</td>
<td>692‡</td>
</tr>
<tr>
<td></td>
<td>24–52</td>
<td>0.10</td>
<td>0.35</td>
<td>0.046</td>
<td>1.44</td>
<td>0.50</td>
<td>320†</td>
</tr>
<tr>
<td>Rosetta</td>
<td>0–24</td>
<td>0.04</td>
<td>0.34</td>
<td>0.040</td>
<td>2.17</td>
<td>-0.85</td>
<td>196</td>
</tr>
<tr>
<td></td>
<td>24–52</td>
<td>0.04</td>
<td>0.37</td>
<td>0.038</td>
<td>3.59</td>
<td>-0.81</td>
<td>1390</td>
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<tr>
<td>Basile et al. (2003)</td>
<td>0–24</td>
<td>0.14</td>
<td>0.22</td>
<td>0.040</td>
<td>1.62</td>
<td>0.50</td>
<td>692‡</td>
</tr>
<tr>
<td></td>
<td>24–52</td>
<td>0.10</td>
<td>0.27</td>
<td>0.026</td>
<td>1.44</td>
<td>0.50</td>
<td>320†</td>
</tr>
<tr>
<td>Hanford</td>
<td>0–24</td>
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<td>0.036</td>
<td>1.63</td>
<td>0.50</td>
<td>160</td>
</tr>
<tr>
<td></td>
<td>24–52</td>
<td>0.02</td>
<td>0.23</td>
<td>0.095</td>
<td>1.15</td>
<td>0.50</td>
<td>66</td>
</tr>
<tr>
<td>Rawls and Brakensiek (1985)</td>
<td>0–24</td>
<td>0.05</td>
<td>0.38</td>
<td>0.138</td>
<td>1.47</td>
<td>0.50</td>
<td>18</td>
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<tr>
<td></td>
<td>24–52</td>
<td>0.04</td>
<td>0.36</td>
<td>0.121</td>
<td>1.52</td>
<td>0.50</td>
<td>15</td>
</tr>
<tr>
<td>Wösten et al. (1999)</td>
<td>0–24</td>
<td>0.01</td>
<td>0.34</td>
<td>0.060</td>
<td>1.41</td>
<td>-1.00</td>
<td>81</td>
</tr>
<tr>
<td></td>
<td>24–52</td>
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<td>0.072</td>
<td>1.50</td>
<td>-0.13</td>
<td>43</td>
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<td>Inverse solution</td>
<td>0–24</td>
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<td>0.131</td>
<td>1.57</td>
<td>0.50</td>
<td>45</td>
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<tr>
<td></td>
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<td>0.06‡</td>
<td>0.26</td>
<td>0.030</td>
<td>1.38</td>
<td>0.50</td>
<td>156</td>
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</table>

‡ $K_s$ value obtained from falling head permeability testing of undisturbed samples.
† Not optimized.

Table 2. The van Genuchten (1980) hydraulic parameters residual and saturated volumetric moisture content ($\theta_r$ and $\theta_s$, respectively), shape-fitting parameters ($\alpha$ and $n$), pore connectivity parameter ($l$), and saturated hydraulic conductivity ($K_s$) for Pit SU10 obtained from various measurement and estimation techniques, including inversion.

<table>
<thead>
<tr>
<th>Source of hydraulic parameters</th>
<th>Depth</th>
<th>RMSE Unscaled</th>
<th>S1</th>
<th>S2</th>
<th>Inverse</th>
</tr>
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<tr>
<td></td>
<td>cm</td>
<td>m$^3$ m$^{-3}$</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Multistep outflow</td>
<td>0–24</td>
<td>0.068</td>
<td>0.010</td>
<td>0.012</td>
<td>0.016</td>
</tr>
<tr>
<td></td>
<td>24–52</td>
<td>0.039</td>
<td>0.024</td>
<td>0.016</td>
<td>0.003</td>
</tr>
<tr>
<td>Rosetta</td>
<td>0–24</td>
<td>0.050</td>
<td>0.006</td>
<td>0.008</td>
<td>0.010</td>
</tr>
<tr>
<td></td>
<td>24–52</td>
<td>0.117</td>
<td>0.028</td>
<td>0.035</td>
<td>0.004</td>
</tr>
<tr>
<td>Basile et al. (2003)</td>
<td>0–24</td>
<td>0.049</td>
<td>0.000</td>
<td>0.000</td>
<td>0.011</td>
</tr>
<tr>
<td></td>
<td>24–52</td>
<td>0.016</td>
<td>0.006</td>
<td>0.006</td>
<td>0.012</td>
</tr>
<tr>
<td>Hanford</td>
<td>0–24</td>
<td>0.044</td>
<td>0.026</td>
<td>0.007</td>
<td>0.015</td>
</tr>
<tr>
<td></td>
<td>24–52</td>
<td>0.020</td>
<td>0.052</td>
<td>0.009</td>
<td>0.003</td>
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<td>Rawls and Brakensiek (1985)</td>
<td>0–24</td>
<td>0.045</td>
<td>0.015</td>
<td>0.011</td>
<td>0.020</td>
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<tr>
<td></td>
<td>24–52</td>
<td>0.059</td>
<td>0.015</td>
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<td>0.016</td>
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<td>0–24</td>
<td>0.052</td>
<td>0.032</td>
<td>0.003</td>
<td>0.018</td>
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<td>0.065</td>
<td>0.014</td>
<td>0.023</td>
<td>0.012</td>
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</tbody>
</table>
adjusted using the second scaling approach (S2), the RMSE$\theta(t)$ values decreased only for the Hanford S2 and MSO S2 curves (0.009 and 0.016 m$^3$ m$^{-3}$, respectively) compared with using the first approach (S1) but increased in the other cases (but not as high as the unscaled values; Table 3, Fig. 4c).

Forward Simulations with Different Soil Hydraulic Property Inputs

Figures 5a to 5c show representative results from simulating infiltration at SU10 from 27 Feb. to 6 May 2003 (DOY 58–126) for the MSO, WOE, and Hanford PTF inputs (results for Rosetta, RB, and Basile inputs not shown). In all cases, the mass balance errors were <0.001%. First, we present the results obtained using the hydraulic parameters obtained from inversion, Basile scaling, and the various PTFs and MSO tests, followed by the results obtained with the scaling inputs, S1 and S2.

The hydraulic parameters obtained from inversion of two short precipitation events yielded the best fit of the $\theta(t)$ data during the extended simulation period with RMSE$\theta(t)$ (Eq. [9]) values ranging from 0.008 to 0.010 m$^3$ m$^{-3}$ and MR$\theta(t)$ (Eq. [10]) values of −0.002 to 0.004 m$^3$ m$^{-3}$ (Table 4, simulation results not shown). These parameter inputs for the profile resulted in a lower RMSE value than the use of the hydraulic parameters derived from the in situ data [RMSE$\theta(t)$ = 0.020 m$^3$ m$^{-3}$] (simulation results not shown).

The Basile scaled parameters yielded a lower RMSE$\theta(t)$ value (0.030 m$^3$ m$^{-3}$) than any of the unscaled PTFs or the unscaled MSO inputs. In this case, $\theta(t)$ values were overestimated for both layers during the entire simulation period (simulation results not shown), as indicated by a MR$\theta(t)$ value of −0.024 m$^3$ m$^{-3}$.

The next best fit of the $\theta(t)$ data was obtained with the Hanford PTF parameter estimates [RMSE$\theta(t)$ = 0.034 m$^3$ m$^{-3}$, MR$\theta(t)$ = −0.002 m$^3$ m$^{-3}$; Table 4, Fig. 5a]. The use of WOE parameters [RMSE$\theta(t)$ = 0.042 m$^3$ m$^{-3}$, MR$\theta(t)$ = −0.005 m$^3$ m$^{-3}$] led to continuous overestimation of moisture content in the shallow layer and underestimation in the deep layer (except for DOY 70, 85, 117, and 125 when the moisture content was overestimated by 3–6%; Table 4, Fig. 5b). When the MSO parameters were used as inputs (Fig. 5c), moisture contents were consistently overestimated in both shallow and deep layers [RMSE$\theta(t)$ = 0.055 m$^3$ m$^{-3}$, MR$\theta(t)$ = −0.053 m$^3$ m$^{-3}$]. This significant overestimation of $\theta(t)$ for both depths is due to the fact that the $\theta(h)$ curves at both depths were shifted toward higher moisture contents than the field curves (Fig. 3a and 4a), as discussed above. The RB and Rosetta parameters yielded the worst fits, with RMSE$\theta(t)$ values of 0.057 and 0.068 m$^3$ m$^{-3}$, respectively (results not shown). Use of the RB parameters resulted in moisture responses that were too

Figure 5. Field-measured moisture contents at two depths and results of direct simulations for Days of the Year (DOY) 58 to 126, 2003. Soil hydraulic parameter inputs obtained from (a) the Hanford pedotransfer function (PTF), (b) the Wösten PTF, and (c) multistep outflow test data using saturated hydraulic conductivity values from falling-head tests. Missing data for DOY 90 to 100 were due to equipment malfunction.
high in the shallow layer and too low in the deep layer, except for 4 d when the moisture content was overestimated. An MR value of −0.015 m³ m⁻³ indicates an overall overestimation of moisture content in both layers. The use of Rosetta parameters led to significant underestimation of θ(t) in the deep layer, with overly dynamic responses to precipitation that resulted in overestimations of >12% on 4 d and a slight underestimation of the θ(t) in the shallow layer. An MR(θ) value of 0.040 m³ m⁻³ reflects this systematic underestimation of moisture content.

Scaling the moisture content inputs by the minimum and maximum field-measured values (Fig. 3b and 4b) improved the RMSEθ(θ) values for the simulations of θ(t) in all cases (Table 4). The RMSEθ(θ) values decreased most significantly with the S1 approach for RosettaS1 (0.031 m³ m⁻³), MSOS1 (0.021 m³ m⁻³), and the RBs1 PTF (0.016 m³ m⁻³). The MR values significantly improved for all estimates (−0.005 to 0.024 m³ m⁻³), except for the HanfordS1 PTF, for which the overestimation of moisture content increased compared with the unscaled approach (MR = −0.018 vs. −0.002 m³ m⁻³; Table 4).

When using the S2 approach, the RMSEθ(θ) value decreased compared with the S1 value only for the HanfordS2 PTF (0.010 vs. 0.022 m³ m⁻³; Table 4). In all other cases (RosettaS2, MSOS2, RBs2, and WOE_S2), the RMSEθ(θ) values were greater than for S1, but not as large as the RMSEθ(θ) values for the unscaled values. The S2 approach yielded an underestimation of moisture content in all cases, with the HanfordS2 PTF estimating the lowest value (MR = 0.003 m³ m⁻³) and the RosettaS2 estimates yielding the highest value (MR = 0.030 m³ m⁻³).

Interestingly, the simulated cumulative water flux leaving at the bottom of the soil profile did not vary significantly when different sets of unscaled hydraulic parameter values were used as inputs. The cumulative flux of water out of the bottom of the domain obtained with the unscaled MSO, Rosetta, RB, and in situ soil hydraulic parameter inputs ranged from −8.4 to −8.7 cm (Table 4) for the extended simulation period. Fluxes estimated with the use of Basile scaling and Hanford PTF inputs were smaller compared with the other four approaches (−7.6 and −7.9 cm), while the smallest fluxes across the bottom of the profile were obtained with the unscaled WOE PTF inputs (−6.9 cm).

The cumulative outflow increased when the S1 inputs were used (−7.5 to −14.0) except for the HanfordS1 parameters; in that case, the flux slightly decreased compared with the value obtained with the unscaled inputs (−7.5 vs. −7.9 cm). With the S2 approach, the cumulative water outflow from the profile increased further for all sets of hydraulic parameter inputs (−8.4 to −14.1 cm).

Simulations performed with the inversely estimated parameters led to higher cumulative water fluxes (−10.7 to −13.6 cm) than those obtained with the other unscaled and scaled inputs, except for the fluxes obtained with the RBs1 and RBs2 parameters (−14.0 and −14.1 cm, respectively; Table 4).

### Discussion

As one might expect, the parameter estimates that yielded the best fits of the in situ θ(h) data also yielded the best simulations of the θ(h) data with time. The unscaled MSO inputs consistently overestimated θ(h), as observed by others. The fits of the various PTFs to the in situ θ(h) curves were variable and not consistent between the shallow and deep sensor locations. For example, the Hanford PTF overestimated θ(h) values at the shallow depth, where it is similar in its ability to fit the data compared with the RB and WOE PTFs, but provided the best fit of the data at the deeper location, where the RB and WOE PTFs did not perform as well. The Rosetta PTF performed poorly at both depths. The Basile scaling approach yielded a relatively poor fit of the data in the shallow layer but gave the best fit of the near-saturated θ(h) values at the deeper sensor location. In all cases except for the Hanford PTF at the deep location, significant improvements in the fit of the estimated θ(h) curves to the in situ measured θ(h) curves were obtained by field scaling the predicted or laboratory-measured saturated and residual moisture contents by the maximum and minimum field-measured θ values, although the improvement was more significant for the shallow layer. The second scaling approach, in which the residual moisture contents are estimated by fitting the retention curve through a point of low moisture content on the retention curve, yielded mixed results in terms of improving the fit of the in situ measured θ(h) curves and only improved the simulations RMSEθ(θ) for the Hanford PTF hydraulic parameter inputs.
We found that accounting for the gravel dead volume with Eq. [3] did not significantly improve the PTF estimates of $\theta_s$ and $\theta_r$ over the uncorrected values. The gravel content of the soil had an appreciable effect on the character of the $\theta(h)$ curve that cannot be accounted for simply by ignoring it or by applying a simple correction factor. The fact that the Basile scaling approach improved the fit of the MSO curve parameters to the in situ data suggests that the differences in applied boundary conditions between the field and laboratory methods did have a significant effect on the retention curves at our study site. These limited results also suggest that the Basile scaling approach, originally applied to instantaneous profile method test data and laboratory evaporation-derivation retention curves, can be successfully extended to in situ measurements of moisture content and pressure head obtained under natural conditions and parameters obtained from MSO data.

The simulation results provide insight into the level of sophistication needed in the hydraulic property inputs to successfully predict soil moisture at two locations in the profile. The soil hydraulic parameters for the profile obtained from inversion of two short rain events in 2003 (24–31 March and 2–6 May, DOY 83–90 and 122–126, respectively) yielded the best predictions of $\theta(t)$ during an extended period (DOY 58–126), but such inversion requires knowledge of the bottom boundary conditions, which are not typically known. Predictions of the retention curves, and consequently the soil moisture predictions using the unscaled RB, WOE, and Rosetta PTFs, were poor; and even though the Hanford PTF performed better, it was not by an appreciable amount. The hydraulic parameter values obtained from laboratory MSO tests yielded no better predictions of soil moisture with time.

We found that simulations of $\theta(t)$ could be significantly improved by simply replacing the saturated and residual moisture contents with the maximum and minimum measured moisture contents, whether the parameters were estimated from PTFs or obtained from MSO measurements. The second scaling approach only improved simulation results when applied to the Hanford PTF.

Water fluxes at the bottom of the soil profile can provide a measure of the potential groundwater recharge, an important quantity in water resources assessment. The simulated cumulative water flux at the bottom of the soil profile generally increased from unscaled to inversely estimated parameter inputs (with the exception of the RB inputs) (Table 4). Although the RMSE values for simulation results with the unscaled, in situ parameters show a good fit of simulated vs. observed soil moisture ($0.020 \text{ m}^3 \text{ m}^{-3}$), the water flux was underestimated by approximately 38% compared with values obtained using the inversely estimated soil hydraulic parameters that were obtained with initial parameters derived from in situ measurements. The simulated water fluxes increased by using the scaled retention curves (S1 and S2) but were still 36 and 31% lower, respectively, than the fluxes obtained with inversely estimated parameters. Thus, in spite of the good fit of simulated vs. observed soil moisture with the use of unscaled or scaled parameters, the water fluxes at the bottom of the profile may be underestimated.

Conclusions

In situ measurements of soil hydraulic properties lead to the best simulations of soil moisture dynamics, but labor, accessibility, and cost issues preclude the conclusion that vadose zone investigations must include numerous colocated moisture and head measurements to facilitate inversion or direct measurement of the in situ moisture retention behavior. We found that the in situ moisture retention behavior at our study site was not well represented by laboratory MSO tests or commonly used PTFs, but that these measures or estimates could be dramatically improved by simply constraining the range of possible moisture contents by the minimum and maximum moisture contents measured in the field. It appears that this method of scaling PTF results can be used to obtain soil hydraulic property inputs of sufficient accuracy for plot-scale modeling efforts without requiring expensive laboratory or in situ tests. The next step is to validate the approach at other locations in the watershed and determine if these values can be scaled up for use in larger scale modeling efforts.

Acknowledgments

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References

1. Physical and mineralogical methods. 2nd ed. SSSA Book Ser. 5. SSSA, Madison, WI.


